

# MATLAB

Introduction, Part II

CS101 Lecture #23

# Administrivia

- ❖ Midterm #2 graded
- ❖ Homework #11 will be due Wed Jan. 4.

- ❖ Midterm #2 graded
- ❖ Homework #11 will be due Wed Jan. 4.
- ❖ Homework #12 will be released over the break, due Friday, Jan 13.

# Warmup Questions

# Question #1

$$\begin{pmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{pmatrix}$$

How can we produce this array?

A  $\text{ones}(3,3) - 2*\text{eye}(3,3)$

B  $\text{ones}(3,3) + 2*\text{eye}(3,3)$

C  $2*\text{ones}(3,3) + \text{eye}(3,3)$

D  $2*\text{ones}(3,3) - \text{eye}(3,3)$

# Question #1

$$\begin{pmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{pmatrix}$$

How can we produce this array?

A  $\text{ones}(3,3) - 2*\text{eye}(3,3)$

B  $\text{ones}(3,3) + 2*\text{eye}(3,3)$

C  $2*\text{ones}(3,3) + \text{eye}(3,3)$

D  $2*\text{ones}(3,3) - \text{eye}(3,3)$  ★

## Question #2

$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$$

How do we access 6 in this array?

- A  $A(2, 1)$
- B  $A(1, 2)$
- C  $A(3, 2)$
- D  $A(2, 3)$



## Question #2

$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{pmatrix}$$

How do we access 6 in this array?

- A A(2, 1)
- B A(1, 2)
- C A(3, 2) ★
- D A(2, 3)

# MATLAB

```
➤ a = [ 1 2 3 ]; %row vector
➤ b = [ 1 2 3 ]'; %column vector
➤ A = [ 1 2 3 ; 4 5 6 ]; %matrix
➤ B = [ a ; b ]; % matrix composition
```

# Matrix-Vector Operations

- ❖ If  $A$  is an  $m \times n$  matrix (i.e., with  $n$  columns), then the product  $Ax$  is defined for  $n \times 1$  column vectors  $x$ . If we let  $Ax = b$ , then  $b$  is an  $m \times 1$  column vector. In other words, the number of rows in  $A$  (which can be anything) determines the number of rows in the product  $b$ .  
[http://mathinsight.org/matrix\\_vector\\_multiplication](http://mathinsight.org/matrix_vector_multiplication)

# Array operations

- Matrix v. elementwise operations:
  - Matrix operations are matrix–vector operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

# Array operations

- Matrix v. elementwise operations:
  - Matrix operations are matrix–vector operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$[ 1 \ 0 \ ; \ 0 \ 1 ] * [ 2 \ 3 ]'$$

# Array operations

- Matrix v. elementwise operations:
  - Matrix operations are matrix–vector operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$\begin{bmatrix} 1 & 0 & ; & 0 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 3 \end{bmatrix}'$$
$$\begin{pmatrix} 1 & 2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2+6 \\ 3+2 \end{pmatrix} = \begin{pmatrix} 8 \\ 5 \end{pmatrix}$$

# Array operations

- Matrix v. elementwise operations:
  - Matrix operations are matrix–vector operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$\begin{bmatrix} 1 & 0 & ; & 0 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 3 \end{bmatrix}'$$
$$\begin{pmatrix} 1 & 2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 2+6 \\ 3+2 \end{pmatrix} = \begin{pmatrix} 8 \\ 5 \end{pmatrix}$$

$$\begin{bmatrix} 1 & 2 & ; & 1 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 3 \end{bmatrix}'$$



# Array operations

- Matrix v. elementwise operations:
  - Elementwise operations are spreadsheet-like operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \times \begin{pmatrix} 2 & 4 \\ 3 & 5 \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 5 \end{pmatrix}$$

# Array operations

- Matrix v. elementwise operations:
  - Elementwise operations are spreadsheet-like operations:

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \times \begin{pmatrix} 2 & 4 \\ 3 & 5 \end{pmatrix} = \begin{pmatrix} 2 & 0 \\ 0 & 5 \end{pmatrix}$$

```
[ 1 0 ; 0 1 ] .* [ 2 4 ; 3 5 ]
```

# Indexing arrays

- ▣ We can index arrays with arrays.

```
A = 0:10:100;  
B = A( [ 5,9,2,2 ] );
```

# Indexing arrays

- We can index arrays with arrays.

```
A = 0:10:100;  
B = A( [ 5,9,2,2 ] );
```

- This permits slicing.

```
A = 0:10:100;  
B = A( 4:7 );
```

# Indexing arrays

➤ In more dimensions:

```
A = [ 1,2,3 ; 4,5,6 ; 7,8,9 ];  
B = A( 1:2,1:2 );  
C = A( :,1:2 );
```

# Multiple returns

- ▣ Functions can return several values.

# Multiple returns

- ▣ Functions can return several values.

```
function [ a,b ] = nonsense( x,y )  
    a = x ^ 2;  
    b = y ^ 3;  
end
```

```
[ q r ] = nonsense( 3,4 )
```

# Plotting

- ▣ `plot` works identically to `plt.plot`.



# Plotting

- ❖ `plot` works identically to `plt.plot`.
- ❖ `figure` creates a new figure (window for plots).

# Plotting

- plot works identically to plt.plot.
- figure creates a new figure (window for plots).

```
x = 0:.1:2*pi;  
y = sin( x );  
figure  
plot( x,y,'o' );  
title( 'sin(x)' );  
xlabel( 'x values' );  
ylabel( 'y values' );
```

# Plotting

- plot works identically to plt.plot.
- figure creates a new figure (window for plots).

```
x = 0:.1:2*pi;  
y = sin( x );  
figure  
plot( x,y,'o' );  
title( 'sin(x)' );  
xlabel( 'x values' );  
ylabel( 'y values' );
```

- MATLAB also supplies an excellent plot editor.

- Here's what we have now:
  - `functions`
  - `array definitions, operations, slicing`
  - `plotting`

- ❖ Here's what we have now:
  - ❑ `functions`
  - ❑ array definitions, operations, slicing
  - ❑ plotting
- ❖ We've seen these parts—what about the rest of our “control structures”?

# Finite difference

```
%% set parameters
alpha = 0.1;
tmax = 0.5;      % maximum time (s)
length = 3.0;   % length of material
dx = 0.2;       % mesh spacing
dt = 0.01;      % time step (s)

%% data storage initialization
t = 0:dt:tmax;   % (s)
x = 0:dx:length; % (m)
u = zeros(numel(t), numel(x)); % Kelvin
```

# Finite difference

```
%% set initial condition
u(1,x>=1&x<=2) = 353.15;           % Kelvin (= 80 deg C)
r = alpha * dt / (dx^2);
s = 1 - 2*r;

%% loop through time steps
for i = 2:1:numel(t)
    for j = 2:1:(numel(x)-1)
        u(i,j) = r*u(i-1,j-1) + s*u(i-1,j) + r*u(i-1,j+1);
    end
end
end
```

- The `for` loop ranges over a set of possible values.



# *for* statement

- ❖ The `for` loop ranges over a set of possible values.
- ❖ This is *not* as flexible as Python's `in` syntax—think of always having to loop over the *index* rather than the item.

# *for* statement

- We create a for loop as follows:
  - `statement for var in range`, where you create `var` and provide `range`
  - one or more statements
  - closing statement `end`

- ❖ We create a for loop as follows:
  - ❑ `statement for var in range`, where you create `var` and provide `range`
  - ❑ one or more statements
  - ❑ closing statement `end`
- ❖ Also have `continue` and `break` available.

## *Example: absolute.m*

```
function [ y ] = absolute( x )
    y = 0;
    if x >= 0
        y = x;
    else
        y = -x;
    end
```

# *if/else statement*

- ❖ We create an if/else statement as follows:
  - ❑ the keyword `if`
  - ❑ a logical comparison (**more on these!**)
  - ❑ a **block** of code

# *if/else statement*

- ❖ We create an if/else statement as follows:
  - ❑ the keyword `if`
  - ❑ a logical comparison (**more on these!**)
  - ❑ a **block** of code
  - ❑ the keyword `elseif` (**note this!**)
  - ❑ a new logical comparison
  - ❑ a different **block** of code

# *if/else statement*

- ❖ We create an if/else statement as follows:
  - ❑ the keyword `if`
  - ❑ a logical comparison (**more on these!**)
  - ❑ a **block** of code
  - ❑ the keyword `elseif` (**note this!**)
  - ❑ a new logical comparison
  - ❑ a different **block** of code
  - ❑ the keyword `else`
  - ❑ a different **block** of code

# *if/else statement*

- ❖ We create an if/else statement as follows:
  - ❑ the keyword `if`
  - ❑ a logical comparison (**more on these!**)
  - ❑ a **block** of code
  - ❑ the keyword `elseif` (**note this!**)
  - ❑ a new logical comparison
  - ❑ a different **block** of code
  - ❑ the keyword `else`
  - ❑ a different **block** of code
  - ❑ the keyword `end`



# Logical statements

- MATLAB does *not* have a `bool` data type.

# Logical statements

- ❖ MATLAB does *not* have a bool data type.
- ❖ Instead of True/False, MATLAB uses integers:
  - ❑ 0 means False
  - ❑ 1 means True

# Logical statements

- ❖ MATLAB does *not* have a bool data type.
- ❖ Instead of True/False, MATLAB uses integers:
  - ❑ 0 means False
  - ❑ 1 means True
- ❖ Available logical operators include:
  - ❑ `<`, `>`, `<=`, `>=`, `==`, `≅`
  - ❑ `&&` for 'and', `||` for 'or'
  - ❑ `ismember` checks equality of elements in arrays.
  - ❑ Also, logical operators as indices!

# Logical statements

- ❖ MATLAB does *not* have a bool data type.
- ❖ Instead of True/False, MATLAB uses integers:
  - ❑ 0 means False
  - ❑ 1 means True
- ❖ Available logical operators include:
  - ❑ `<`, `>`, `<=`, `>=`, `==`, `≅`
  - ❑ `&&` for 'and', `||` for 'or'
  - ❑ `ismember` checks equality of elements in arrays.
  - ❑ Also, logical operators as indices!
  - ❑ `A( A<0 )`

❖ Saving data uses `save`:

```
A = [ 1 2 3 ; 4 5 6 ];  
save( 'test', 'A' );
```

- ❖ Saving data uses `save`:

```
A = [ 1 2 3 ; 4 5 6 ];  
save( 'test', 'A' );
```

- ❖ Note that the *string* version of the variable name is required!

- ❖ `load` also useful:

```
A = load( 'test', 'A' );
```

▣ A more advanced tool: `importdata`

```
data = importdata( 'rainfall.txt' );
```

- ▣ A more advanced tool: `importdata`

```
data = importdata( 'rainfall.txt' );
```

- ▣ Can be used to process CSVs.



- ❖ A more advanced tool: `importdata`

```
data = importdata( 'rainfall.txt' );
```

- ❖ Can be used to process CSVs.
- ❖ Old process using `fopen`, `fscanf`, `fclose`, `fprintf` also common.

- ▣ Images can also be opened as files.

```
A = importdata( 'rabbit-bw.jpg' );  
image( A );
```

- ❖ Images can also be opened as files.

```
A = importdata( 'rabbit-bw.jpg' );  
image( A );
```

- ❖ Black and white images are arrays of 0s and 1s.
- ❖ Greyscale images are values from 0 and 1.
- ❖ Color images are three-dimensional arrays.  
(Why?)
- ❖ Variations exist depending on the underlying data.